Towards Comprehensive Modelling Approach and Consistent Behavioural Assumptions for Activity-Based Travel Demand Model: A Random Utility Maximizing Activity Scheduling Model<br>Khandker M. Nurul Habib, Ph.D., P.Eng.<br>Assistant Professor, Department of Civil \& Environmental Engineering<br>University of Alberta<br>Khandker.nurulhabib@ualberta.ca

## 1. Introduction

Although activity-based approach to travel demand modelling was introduced three decades ago, the conventional trip-based models are still in use for practical policy investigation in almost everywhere with very few exceptions. The main reason of such failure is the lack of comprehensive modelling framework with consistent behavioural assumptions that can completely replace well-structure trip-based four-stage model. Many issues related to the modeling framework, such as the concept of activity utility, application of so-called rules, modeling time frame (daily versus weekly), and time discretization are still under debate in the research community. The only significant consensus that has been apparently reached so far is the recognition of two general components for an activity-based travel demand model: the activity generation component and the activity scheduling-rescheduling component (Habib and Miller, 2009). There is now significant interest among researchers in capturing the dynamic behavioural process of these two components within comprehensive modelling framework under consistent behavioural assumption, e.g. Random Utility Maximization (RUM). Habib and Miller (2008) presented RUM-based models of activity generation processes. However, to date no such unified econometric model is available for the activity scheduling process. In an effort to address this issue, an econometric model for the activity scheduling process based on RUM is proposed in this paper.

The proposed modeling framework exploits the RUM-based approach to modeling activity scheduling process by considering the dynamics of the time budget constraint over the course of a day. The unique feature of the proposed model is that it does not need to discretize the time. Econometrically the proposed model is a dynamic RUM-based Joint discrete continuous model. For empirical investigation, the proposed framework is applied for weekend activity scheduling using 2002-2003 CHASE (Computerized Household Activity Scheduling Elicitor) survey data collected in Toronto, Canada.

## 2. RUM-Based Activity Scheduling Model

Let us consider that an individual, $i$, at a particular point in the day is to choose an activity type and corresponding time expenditure, $t_{j}$. In expending time for the chosen activity, however, the individual faces a time budget limitation. This time budget limitation is not constant throughout the day. The day begins with a 24 -hour time budget limitation, which is gradually reduced with the number of activities performed over the course of the day. The remaining time budget at any point of scheduling an activity is the left over time after all previously performed activities have been completed. While executing an activity, i.e., defining the duration of a specific activity, the individual trades off between time expenditure to the chosen activity versus total time left over for all other activities to be completed in the balance of the day. As we do not know for certain
the causes and factors that influence the individual's tradeoffs in choosing alternative activity types and time expenditures out of a limited time budget, it is reasonable to consider the assumption that the utility associated with activity type and time expenditure includes random elements. Hence, the utility maximizing approach to model activity type choice and time expenditure choice is really a Random Utility Maximizing (RUM) approach. Addressing the facts that the time budget decreases as the day progresses and that the scheduling of any particular activity type is affected by what activities the individual already completed in a given day ensures that the method will capture the true behavioral dynamics of the activity scheduling process. In the context of such a situation the choice of a given activity type at any point in time influences expenditures of the limited amount of time from the left over time budget, and vice versa.


Figure 1: Dynamic Discrete-Continuous Approach to Model Activity Pattern Formation
Figure 1 presents the schematic diagram of such a prototype example of the activity scheduling choice process. This is an example of a single day modeling framework. In the case of a multiday scheduling process the end of day activity of the previous day is regarded as the first activity of the following day. However, in the case of a single day (a 24 -hour time span) model this may or may not be true. In this paper we are presenting a single-day activity scheduling model, where the scheduling process begins at midnight $(t=0)$ and continues until the end of the day. For a 24hr modeling timeframe such temporal referencing is unavoidable, even though it creates left and right censoring issues for the first and last activities. However, beginning at the reference time $(t=0)$ different people might perform different numbers and types of activities before the end of the day and thereby may have different types of activity patterns. The proposed approach does
not consider different activity patterns as alternatives, rather it models the scheduling process, so that the activity pattern evolves out of the dynamic scheduling process.

## 3. Econometric Model Formulation

From a modeling point of view the challenge is that the dynamics of activity scheduling and correlation between activity type choice and corresponding time allocation are sufficiently captured in the RUM-based model formulation.

### 3.1 Formulation of Utility Function

let us assume that the utility function of the individual person, $i$, for the $j$ alternative activity type choice is:
$U_{j}=V_{j}+\varepsilon_{j}=\beta_{j} x_{j}+\varepsilon_{j} \quad ; j=1,2,3, \ldots \ldots \ldots . A$
Where $V_{j}$ is the systematic utility, $x_{j}$ is a set of explanatory variables, $\beta_{j}$ is corresponding parameter vector and $\varepsilon_{j}$ is the random term. Similarly, let us assume that the total direct utility function of the same individual for time expenditure, $\left(t_{k}\right)$ in chosen activity is (Bhat, 2008):

$$
\begin{equation*}
U\left(t_{k}\right)=\sum_{k=1}^{2} \frac{\gamma_{k}}{\alpha_{k}}\left[\exp \left(\psi_{k} z_{k}+\varepsilon_{k}^{\prime}\right)\right]\left\{\left(\frac{t_{k}}{\gamma_{k}}+1\right)^{\alpha_{k}}-1\right\} \tag{2}
\end{equation*}
$$

Here $k=1$ indicates the chosen activity and $k=2$ indicates the remainder of the amount of time (the composite activity) under the available time budget. The component, $\exp \left(\psi_{k} z_{k}+\varepsilon_{k}\right)$, is the baseline utility function. In the baseline utility function, $z_{k}$ indicates a vector of explanatory variables; $\Psi_{k}$ indicates a vector of coefficient corresponding to $z_{k}$; and $\varepsilon_{k}^{\prime}$ is the unobserved random error component of the random utility function. Among other components of the utility function, $\alpha_{k}$ is the satiation parameter and $\gamma_{k}$ is the translation parameter. If the total time budget available is given by $T$, then the time allocation decision becomes an optimization problem under time budget constraints:
$t_{j}+t_{c}=T$
Here the subscript, ${ }_{j}$, indicates the time allocated to the current chosen activity while ${ }_{c}$ indicates the time left over for the composite. By using the Lagrangian function we get:

$$
\begin{equation*}
l=\sum_{k=1}^{2} \frac{\gamma_{k}}{\alpha}\left[\exp \left(\psi_{k} z_{k}+\varepsilon_{k}^{\prime}\right)\right]\left\{\left(\frac{t_{k}}{\gamma_{k}}+1\right)^{\alpha}-1\right\}-\lambda\left[\sum_{k=1}^{2} t_{k}-T\right] \tag{4}
\end{equation*}
$$

Here $\mathrm{k}=1,2$ refer to j and c
Here $\lambda$ is the Lagrangian multiplier. According to the first-order Kuhn-Tucker optimality condition (Kuhn and Tucker, 1951), the generalized expression can be written as:
$\left[\exp \left(\psi z+\varepsilon^{\prime}\right)\right]\left\{\left(\frac{t}{\gamma}+1\right)^{\alpha-1}\right\}-\lambda=0$, if $t=t_{k}, k=1,2$
$\left[\exp \left(\psi z+\varepsilon^{\prime}\right)\right]\left\{\left(\frac{t}{\gamma}+1\right)^{\alpha-1}\right\}-\lambda<0$, if $t<t_{k}, k=1,2$
Considering the composite activity as the reference activity ( $k=c$ ) for time allocation and given the circumstance that composite activity time allocation is a non-zero value, we can specify $\lambda$ as a function of the composite activity function:

$$
\begin{equation*}
\lambda=\left[\exp \left(\psi_{c} z_{c}+\varepsilon_{c}^{\prime}\right)\right]\left\{\left(\frac{t_{c}}{\gamma_{c}}+1\right)^{\alpha-1}\right\} \tag{7}
\end{equation*}
$$

Substituting $\lambda$ in the Kuhn-Tucker optimality conditions we can specify that for a case of $t_{j}>0$ :
$\left.\left.\left[\exp \left(\psi_{j} z_{j}+\varepsilon_{j}^{\prime}\right)\right]\right\}\left\{\left(\frac{t_{j}}{\gamma_{j}}+1\right)^{\alpha-1}\right\}-\left[\exp \left(\psi_{c} z_{c}+\varepsilon_{c}^{\prime}\right)\right]\right\}\left\{\left(\frac{t_{c}}{\gamma_{c}}+1\right)^{\alpha-1}\right\}=0$
$\left[\exp \left(\psi_{j} z_{j}+\varepsilon_{j}^{\prime}\right)\right]\left\{\left(\frac{t_{j}}{\gamma_{j}}+1\right)^{\alpha-1}\right\}=\left[\exp \left(\psi_{c} z_{c}+\varepsilon_{c}^{\prime}\right)\right]\left[\left(\frac{t_{c}}{\gamma_{c}}+1\right)^{\alpha-1}\right\}$
Taking the logarithm of both sides:
$\left(\psi_{j} z_{j}+\varepsilon_{j}^{\prime}\right)+(\alpha-1) \ln \left(\frac{t_{j}}{\gamma_{j}}+1\right)=\left(\psi_{c} z_{c}+\varepsilon_{c}^{\prime}\right)+(\alpha-1) \ln \left(\frac{t_{c}}{\gamma_{c}}+1\right)$
$\left[\psi_{j} z_{j}+(\alpha-1) \ln \left(\frac{t_{j}}{\gamma_{j}}+1\right)\right]+\varepsilon_{j}^{\prime}=\left[\psi_{c} z_{c}+(\alpha-1) \ln \left(\frac{t_{c}}{\gamma_{c}}+1\right)\right]+\varepsilon_{c}^{\prime}$
$V_{j}^{\prime}+\varepsilon_{j}^{\prime}=V_{c}^{\prime}+\varepsilon_{c}^{\prime}$
The above condition of equality applies to an expenditure of $t_{j}$ amount of time on the given activity. Similarly, for the case where $t<t_{j}$
$V_{j}^{\prime}+\varepsilon_{j}^{\prime}<V_{c}^{\prime}+\varepsilon_{c}^{\prime}$
Here, the systematic utility component of activity time allocation is
$V_{k}^{\prime}=\left[\psi_{k} z_{k}+(\alpha-1) \ln \left(\frac{t_{k}}{\gamma_{k}}+1\right)\right], k=j, c$
Now to derive the probability function of spending a specific amount of time, $\left(t_{2}\right)$, we can further modify Equation (8) (Bhat, 2008)
$\varepsilon_{j}^{\prime}-\varepsilon_{c}^{\prime}=V_{c}^{\prime}-V_{j}^{\prime}$ for $t=t_{j}$
$\varepsilon_{j}^{\prime}-\varepsilon_{c}^{\prime}<V_{c}^{\prime}-V_{j}^{\prime}$ for $t<t_{j}$

### 3.2 Assumption of Error Term Distributions and Deriving Probability Distribution Functions

 According to RUM theory, an alternative activity, $j$, will be chosen if the utility of that alternative activity is the maximum of all considered alternatives.$$
\begin{aligned}
& U_{j}>\max _{n=1,2,3 \ldots . . . A, n \neq j} U_{n} \\
& V_{j}>\left\{\begin{array}{c}
\max \\
n=1,2,3 \ldots . . . . A, n \neq j
\end{array} U_{n}\right\}-\varepsilon_{j}
\end{aligned}
$$

So,

$$
\begin{align*}
\operatorname{Pr}\left(U_{j}>\max _{n=1,2,3 \ldots . . . A, n \neq j}\right. & \left.U_{n}\right)=\operatorname{Pr}\left(V_{j}>\left\{\begin{array}{c}
\max \\
n=1,2,3 \ldots . . . M, n \neq j
\end{array} U_{n}\right\}-\varepsilon_{j}\right) \\
& =\operatorname{Pr}\left(V_{j}>\left(V_{n}+\varepsilon_{n}\right)-\varepsilon_{j}\right)  \tag{10}\\
& =\operatorname{Pr}\left(V_{n}<V_{j}+\left(\varepsilon_{j}-\varepsilon_{n}\right)\right)
\end{align*}
$$

Let us assume that the random variable, $\varepsilon_{j}$, has the IID Type I Extreme-Value distribution with a mean value of 0 and a scale parameter of 1 . Hence, the implied cumulative distribution of the random error term of the chosen alternative, $F\left(\varepsilon_{A}\right)$, can be written as (Ben-Akiva and Lerman, 1985; Lee, 1983; Train, 2003):

$$
\begin{align*}
& \operatorname{Pr}\left(\varepsilon_{n}<V_{j}-V_{n}+\varepsilon_{j}\right)=\frac{\exp \left(V_{j}\right)}{\exp \left(V_{j}\right)+\sum_{n \neq j} \exp \left(V_{n}\right)}=\frac{\exp \left(\beta_{j} x_{j}\right)}{\exp \left(\beta_{j} x_{j}\right)+\sum_{n \neq j} \exp \left(\beta_{n} x_{n}\right)} \\
& \therefore F\left(\varepsilon_{j}\right)=\frac{\exp \left(V_{j}\right)}{\exp \left(V_{j}\right)+\sum_{n \neq j} \exp \left(V_{n}\right)}=\frac{\exp \left(\beta_{j} x_{j}\right)}{\exp \left(\beta_{j} x_{j}\right)+\sum_{n \neq j} \exp \left(\beta_{n} x_{n}\right)} \tag{11}
\end{align*}
$$

For the time allocation model of chosen activity, as shown in Equation (9), let us assume the similar distribution assumption for the random error component, $\varepsilon_{j}^{\prime}$, to be an IID Type I ExtremeValue distribution with a mean value of 0 and a scale parameter of $\sigma$. Since the time allocation follows the discrete activity type choice, the time allocation is concerned with two alternative options (the chosen activity and the composite activity). According to RUM theory, (considering the time budget constraints and the Kuhn-Tucker optimality condition), the time allocation, $t_{j}$, to the chosen activity depends on the condition shown in Equation (9). As mentioned above, the difference between two IID Extreme-Value random terms is logistically distributed. Moreover, the probability distribution function (PDF) and cumulative distribution function (CDF) of $\varepsilon_{j}^{\prime}$ are given by (Johnson et al., 1995):

$$
\begin{align*}
& \operatorname{Pr}\left(\varepsilon_{j}^{\prime}=\left(V_{c}^{\prime}-V_{j}^{\prime}\right)+\varepsilon_{c}^{\prime}\right)=\frac{1}{\sigma} \exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\left[1+\exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\right]^{-2} \\
& \operatorname{Pr}\left(\varepsilon_{j}^{\prime}<\left(V_{c}^{\prime}-V_{j}^{\prime}\right)+\varepsilon_{c}^{\prime}\right)=\left[1+\exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\right]^{-1} \tag{12}
\end{align*}
$$

To ensure model identification, the specification of $V_{j i}^{\prime}$ and $V_{c i}^{\prime}$ can be further specified as (Bhat, 2008):

$$
\begin{align*}
& V_{j}^{\prime}=\left[\psi_{j} z_{j}+(\alpha-1) \ln \left(\frac{t_{j}}{\gamma_{j}}+1\right)\right] \\
& \text { and }  \tag{13}\\
& V_{c}^{\prime}=(\alpha-1) \ln \left(t_{c}\right)
\end{align*}
$$

Here $V_{c i}^{\prime}$ indicates the composite activity for the corresponding chosen activity type under remaining time budget constraints. Now, according to the change of variables theorem, the probability distribution function (PDF) can be determined as follows:

$$
\begin{aligned}
\operatorname{Pr}\left(t=t_{j}\right) & =\left(\frac{\delta\left(\left(V_{c}^{\prime}-V_{j}^{\prime}\right)\right)}{\delta t_{j}}\right) \frac{1}{\sigma} \exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\left[1+\exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\right]^{-2} \\
& =\left(\frac{1-\alpha}{t_{j}+\gamma_{j}}+\frac{1-\alpha}{t_{c}}\right) \frac{1}{\sigma} \exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\left[1+\exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\right]^{-2}
\end{aligned}
$$

where,

$$
\begin{aligned}
& \left(\frac{\delta\left(\left(V_{c}^{\prime}-V_{j}^{\prime}\right)\right)}{\delta t_{j}}\right)=\frac{\delta}{\delta t_{j}}\left((\alpha-1) \ln \left(T-t_{j}\right)-\psi z-(\alpha-1) \ln \left(t_{j} / \gamma_{j}+1\right)\right) \\
& \quad=\frac{(1-\alpha)}{t_{j}+\gamma_{j}}+\frac{(1-\alpha)}{t_{c}}
\end{aligned}
$$

And

$$
\begin{align*}
& \operatorname{Pr}\left(t<t_{j}\right)=\left[1+\exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\right]^{-1}  \tag{15}\\
& \therefore F\left(\varepsilon_{j}^{\prime}\right)=\left[1+\exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\right]^{-1}
\end{align*}
$$

### 3.3 Joint Probability of Activity Type Choice and Time Allocation

For joint estimation of RUM-based activity type choice and time allocation model, let us consider that the transformed error terms are bivariate normal distributes. As per Lee (1983), the transformed error terms are:

$$
\begin{align*}
\varepsilon_{j}^{*} & =J_{1}\left(\varepsilon_{j}\right)=\Phi^{-1}\left[F\left(\varepsilon_{j}\right)\right]  \tag{17}\\
\varepsilon_{k}^{*} & =J_{2}\left(\varepsilon_{j}^{\prime}\right)=\Phi^{-1}\left[F\left(\varepsilon_{j}^{\prime}\right)\right]
\end{align*}
$$

These transformed error terms are correlated with correlation factor $\rho_{j t}$ : $\operatorname{BVN}\left[J_{l}\left(\varepsilon_{j}\right), J\left(\varepsilon_{j}^{\prime}\right), \rho_{j t}\right]$. So,
$\operatorname{Pr}\left(\right.$ Time $=t_{j} \cap$ Activity Type $\left.=j\right)=\operatorname{Pr}\left(\right.$ Time $\left.=t_{j} \cap \varepsilon \leq J_{1}\left(\varepsilon_{j}\right)\right)$

$$
\begin{equation*}
=\left(\frac{1-\alpha}{t_{j}+\gamma_{j}}+\frac{1-\alpha}{t_{c}}\right) \frac{1}{\sigma} \exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\left[1+\exp \left(\frac{-\left(V_{c}^{\prime}-V_{j}^{\prime}\right)}{\sigma}\right)\right]^{-2} \Phi\left(\frac{\left.J_{1}\left(\varepsilon_{j}\right)-\rho_{j i t} J_{2}\left(\varepsilon_{j}^{\prime}\right)\right]}{\sqrt{1-\rho_{j t}^{2}}}\right) \tag{18}
\end{equation*}
$$

Based on the above formulation, the likelihood function, $L_{i}$, of an individual observation, $i$, can be written as:
$L_{i}=\prod_{j=1}^{A}\binom{\left.\left(\frac{1-\alpha}{t_{j i}+\gamma_{j i}}+\frac{1-\alpha}{t_{c i}}\right) \frac{1}{\sigma} \exp \left(\frac{-\left(V_{c i}^{\prime}-V_{j i}^{\prime}\right)}{\sigma}\right)\left[1+\exp \left(\frac{-\left(V_{c i}^{\prime}-V_{j i}^{\prime}\right)}{\sigma}\right)\right]^{-2}\right)^{D_{j i}}}{\Phi\left(\frac{\left.J_{1}\left(\varepsilon_{j i}\right)-\rho_{j i t} J_{2}\left(\varepsilon_{j i}^{\prime}\right)\right]}{\sqrt{1-\rho_{j t}^{2}}}\right)}$
$\mathrm{D}_{\mathrm{ji}}$ is a binary indicator variable for the chosen activity type

Here $D_{j i}$ is a binary indicator variable for the chosen alternative activity. Now if we consider the sequence of activity selection and corresponding time allocation, i.e., the activity scheduling process for 24-hour time period, the joint likelihood function of the complete schedule of an individual, $i$, , becomes:

$$
L_{T i}=\prod_{Z=1}^{S}\left[\prod_{j=1}^{A}\left(\begin{array}{c}
\left.\left(\frac{1-\alpha}{t_{j i}+\gamma_{j i}}+\frac{1-\alpha}{t_{c i}}\right) \frac{1}{\sigma} \exp \left(\frac{-\left(V_{c i}^{\prime}-V_{j i}^{\prime}\right)}{\sigma}\right)\left[1+\exp \left(\frac{-\left(V_{c i}^{\prime}-V_{j i}^{\prime}\right)}{\sigma}\right)\right]^{-2}\right)^{D_{j i}}  \tag{20}\\
\\
\Phi\left(\frac{\left.J_{1}\left(\varepsilon_{j i}\right)-\rho_{j i} J_{2}\left(\varepsilon_{j i}^{\prime}\right)\right]}{\sqrt{1-\rho_{j t}^{2}}}\right)
\end{array}\right]_{Z}\right.
$$

Here $S$ is the total number of activities performed in the 24 -hour time period. Now, if we have a sample of observation with sample size, $N$, the joint likelihood function for the sample, $L$, becomes:
$L=\prod_{i=1}^{N} L_{T i}$
This expression is a likelihood function of a dynamic RUM discrete-continuous model. It is of a closed form and can be estimated using classical Maximum Likelihood Estimation (MLE) algorithms.

## 4. Data for Empirical Investigation

CHASE survey data from the first wave of the Toronto Travel-Activity Panel survey
(TAPS) are used in this paper for empirical modeling of weekend activity scheduling (Doherty et al, 2004). The CHASE survey was conducted in Toronto in 2002-2003 among 426 individuals in 271 households. After cleaning the dataset for missing information, a total of 423 individuals from 264 households were selected for the sample to estimate the empirical model. In this dataset activities are classified into 9 general types: Basic Needs, Work/School, Household Obligation, Drop/Pick, Shopping, Recreational, Social and Other. Now, if we define the scheduling of an activity type at any point in time as a scheduling cycle, then the observed weekend schedules are composed of a minimum of 3 cycles and a maximum of 30 cycles and the average number of scheduling cycles is 12 .

## 5. Empirical Model of Weekend Activity Scheduling

The modeling begins with activity type choice at the beginning of the day, and the corresponding time expenditures are monitored. At the end of the first activity, the same process of type selection and corresponding time expenditure follows until the end of the day. The process of choosing an activity and consequent time expenditure may be referred as scheduling steps or scheduling cycle. At every scheduling step in the continuous time expenditure model component, we consider the trade-off in time expenditure to the specific chosen activity type, with respect to the leftover time for the composite activity.

The estimated model parameters are presented in Table 1. Several types of variables are considered in the model estimation process. These include socio-economic, residential location, transportation system performance, and activity specific attributes. The complicated structure of the model and the intention of joint estimation of a dynamic 24-hour activity scheduling process
posed a significant challenge in parameter estimation for the given sample of data. However, surprisingly, it was found that the estimation process is fairly efficient and a large number of parameters (106 parameters) can be estimated using even a small sample. This is an indication of the behavioural validity of the modeling structure. It proves that the econometric modeling structure fits well with the observed dynamic scheduling formation process.

A series of specifications were tested and, after removing insignificant parameters in different combinations of variable specifications, the final specification (presented in Table 1) was reached. In terms of variables, similar variables entered into the systematic part of the activity type choice utility function and the baseline utility function of the continuous time expenditure model component. In addition to the accommodation of self-selection effects in activity type selection for scheduling and corresponding time expenditure, an unrestricted correlation between unobserved factors influencing activity type choice and time expenditure is accommodated. The goodness-of-fit of the estimated model is calculated using the adjusted rho-square value of 0.1 , which is reasonable for such a complicated model structure.

## 6. Direction for Future Research

Future application of this modeling framework for weekday or complete weekday-weekend scheduling behaviour will be explored. Finally, many variables related to activity location and inter-household interactions are incorporated as exogenous variables in this paper. It is important to incorporate activity location choice within this modeling framework. Similarly, interhousehold interactions and travel mode choice (if a trip is necessary in order to arrive at the location of the activity) are also important. It is understood that integration of the activity scheduling model with an activity generation model would resolve issues related to modeling timeframe (typical day versus week-long model). All of these factors pose methodological challenges and hence are taken into account in recommendations for further research.

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Table 1: Estimated Parameters of Weekend Activity Scheduling Model Activity type Choice Model Component

| Variables | Activity Type | Parameter | t-Statistics |
| :---: | :---: | :---: | :---: |
| Constant |  |  |  |
|  | Household Obligations | -2.1392 | -5.155 |
|  | Drop off/Pick up | -3.6148 | -22.471 |
|  | Shopping | -3.4814 | -19.992 |
|  | Services | -3.6015 | -12.206 |
|  | Other | -1.4744 | -2.197 |
| Star Time in Hours from Mid Night |  |  |  |
|  | Work/School | -0.1055 | -9.778 |
|  | Drop off/Pick up | -0.0238 | -1.591 |
|  | Services | -0.0414 | -1.861 |
|  | Recreation/Entertainment | 0.068 | 11.61 |
|  | Other | 0.0536 | 4.858 |
| Number of Activities already Performed from beginning of the day |  |  |  |
|  | Basic Needs | -0.0934 | -11.99 |
|  | Work/School | 0.0838 | 4.73 |
|  | Drop off/Pick up | 0.0462 | 2.127 |
|  | Shopping | 0.0568 | 3.708 |
|  | Services | 0.0554 | 1.689 |
|  | Social | 0.0844 | 5.98 |
| Total Travel Time (Minutes) Required to go the Activity Location from the previous ActivityLocation |  |  |  |
|  | Basic Needs | -0.0716 | -22.228 |
|  | Work/School | 0.0065 | 3.557 |
|  | Household Obligations | -0.0502 | -12.548 |
|  | Recreation/Entertainment | -0.0301 | -11.021 |
|  | Other | -0.0272 | -5.435 |
| Household Size: Number of People in the Household |  |  |  |
|  | Work/School | -0.1001 | -2.629 |
|  | Household Obligations | -0.09 | -2.742 |
|  | Shopping | -0.0746 | -1.739 |
|  | Recreation/Entertainment | -0.1511 | -6.723 |
|  | Social | -0.2036 | -5.246 |
|  | Other | -0.1678 | -3.678 |
| Logarithm of Age in Years |  |  |  |
|  | Work/School | -0.4985 | -9.374 |
|  | Household Obligations | 0.242 | 2.265 |
|  | Recreation/Entertainment | -0.583 | -19.243 |
|  | Social | -0.9811 | -13.203 |
|  | Other | -0.4025 | -2.349 |

Table 1 (Continue)

| Gender: Male |  |  |
| :---: | :---: | :---: |
| Work/School | 0.3301 | 3.913 |
| Household Obligations | -0.5607 | -7.669 |
| Logarithm of Yearly Income in Canadian Dollars (2002-2003) |  |  |
| Work/School | 0.0276 | 1.896 |
| Household Obligations | -0.0246 | -2.377 |
| Services | -0.0328 | -1.422 |
| Social | 0.0426 | 2.152 |
| Other | -0.0458 | -2.738 |
| Number of Automobile in Household |  |  |
| Recreation/Entertainment | 0.0943 | 2.206 |
| Employment Status: Non-Full Time Job |  |  |
| Household Obligations | 0.1645 | 2.147 |
| Recreation/Entertainment | 0.1167 | 1.867 |
| Social | 0.3476 | 2.899 |
| Number of Children in Household |  |  |
| Work/School | 0.0808 | 1.501 |
| Household Obligations | 0.2999 | 7.411 |
| Drop off/Pick up | 0.3959 | 8.791 |
| Time Expenditure Model Component |  |  |
| Constant |  |  |
| Basic Needs | -1.8765 | -5.583 |
| Star Time in Hours from Mid Night |  |  |
| Work/School | 0.0355 | 1.95 |
| Household Obligations | 0.0441 | 2.965 |
| Drop off/Pick up | 0.3274 | 10.362 |
| Shopping | 0.1742 | 5.58 |
| Services | 0.1753 | 2.251 |
| Recreation/Entertainment | 0.3276 | 22.311 |
| Social | 0.2699 | 9.087 |
| Other | 0.1768 | 9.427 |
| Number of Activities already Performed from beginning of the day |  |  |
| Basic Needs | 0.1509 | 17.353 |
| Household Obligations | -0.0516 | -2.532 |
| Drop off/Pick up | -0.0806 | -2.144 |
| Social | -0.0711 | -2.209 |

Table 1 (Continue)

| Total Travel Time (Minutes) Required to go the Activity Location from the previous ActivityLocation |  |  |
| :--- | ---: | ---: |
| Household Obligations | 0.0104 | 2.492 |
| Drop off/Pick up | 0.0513 | 6.057 |
| Shopping | 0.0517 | 5.217 |
| Services | 0.0482 | 4.001 |
| Recreation/Entertainment | 0.0102 | 4.469 |
| Social | 0.012 | 3.707 |
| Other | 0.0194 | 2.659 |
| Household Size: Number of People in the Household |  |  |
| Work/School | 0.1257 | 3.056 |
| Household Obligations | -0.4742 | -10.303 |
| Drop off/Pick up | -0.2259 | -3.044 |
| Recreation/Entertainment | -0.1875 | -5.985 |
| Logarithm of Age in Years |  |  |
| Basic Needs | -0.5918 | -6.335 |
| Work/School | -0.8989 | -10.003 |
| Drop off/Pick up | -3.7314 | -18.392 |
| Shopping | -2.8777 | -14.043 |
| Services | -2.2708 | -7.123 |
| Recreation/Entertainment | -2.3568 | -23.922 |
| Social | -1.7052 | -12.407 |
| Other | -2.0626 | -14.248 |
| Logarithm of Yearly Income in Canadian Dollars (2002-2003) |  |  |
| Basic Needs | 0.0576 | 6.154 |
| Work/School | 0.0348 | 1.624 |
| Household Obligations | -0.1508 | -11.12 |
| Services | -0.0598 | -1.416 |
| Recreation/Entertainment | 0.036 | 2.565 |
| Logarithm of Duration (Years) of Living in the City |  |  |
| Household Obligations | -0.2229 | -2.752 |
| Shopping | 0.2225 | 3.488 |
| Recreation/Entertainment | 0.1902 | -11.314 |
| Other | 0.1383 | 2.933 |
| Nousehold Obligations | 0.2402 | 2.388 |

Table 1 (Continue)

| Employment Status: Non-Full Time Job |  |  |
| :---: | :---: | :---: |
| Work/School | -1.0015 | -7.129 |
| Social | -0.7831 | -4.078 |
| Other | -0.6725 | -3.352 |
| Number of Children in Household |  |  |
| Household Obligations | 0.2439 | 3.842 |
| Satiation Parameter |  |  |
| Constant |  |  |
| Work/School | -0.5267 | -7.774 |
| Household Obligations | -0.2286 | -8.922 |
| Drop off/Pick up | -0.8955 | -18.893 |
| Shopping | -0.7234 | -14.907 |
| Services | -0.8185 | -4.594 |
| Recreation/Entertainment | -0.696 | -14.596 |
| Social | -0.5025 | -4.942 |
| Other | -0.3139 | -6.312 |
| Star Time in Hours from Mid Night |  |  |
| Work/School | 0.0215 | 3.983 |
| Services | 0.0234 | 1.84 |
| Recreation/Entertainment | 0.0285 | 10.926 |
| Social | 0.0271 | 4.551 |
| Correlation Coefficient Between Activity Type Choice and Time Expenditure |  |  |
| Constant | -0.1942 | -8.419 |
| Loglikelihood of Full model |  | 501.158 |
| Loglikelihood of Constant-Only Model |  | 732.032 |
| Adjusted Rho-Square Value |  | 0.1 |

